



Numerical Simulation of the Interaction between a Free-flying Ring and a Curved Shock Wave

DLR Results of the ESA ATD3-Workshop 2022

Bodo Reimann¹

Abstract

A free-flying ring crossing the curved bow shock in front of cylinder was selected as numerical test case within ESA's Aerothermodynamics & Design for Demise working group in 2022. The experiment to compare with was carried out in the VKI Longshot gun tunnel facility at a free stream Mach number of about 14. This paper presents the DLR simulation results achieved by coupling the DLR in-house CFD solver TAU with a 6-DoF flight mechanic solver. Local dynamic grid adaptation is used to capture shocks and unsteady shock interactions. The results of the coupled simulation are compared to results of a simulation with prescribed motion using the experimental determined motion state as input, and results of a flight mechanic simulation prescribing the measured aerodynamic forces and moments. Both the coupled and the forced motion simulation show similar values for the aerodynamic loads but higher than the measured ones. The flight mechanic simulation shows good agreement with the VKI experiments.

Keywords: *CFD 6-DoF coupling, space debris, free-flight modeling, shock interaction, ATD3-Workshop*

Nomenclature

Abbreviations

ATD3	Aerothermodynamics & Design for Demise
CFD	Computational fluid dynamics
CoG	Center of gravity
DLR	German Aerospace Center
6-DoF	Six degree of freedom
RBD	Rigid body dynamics
VKI	von Karman Institute for Fluid Dynamics

Latin

C_L	Lift coefficient
C_D	Drag coefficient
C_m	Pitching moment coefficient
C_p	Pressure coefficient
D	Drag
\vec{F}	Force vector $\vec{F} = (F_x, F_y, F_z)$
\vec{g}	Gravitational acceleration
\bar{I}	Inertia tensor $\bar{I} = I_{ij}$
L	Lift
\vec{M}	Moments vector $\vec{M} = (M_x, M_y, M_z)$

M	Mach number
m	Mass
p	Pressure
T	Temperature
t	Time
\vec{x}	Position vector $\vec{x} = (x, y, z)$
$\dot{\vec{x}}$	Velocity vector $\dot{\vec{x}} = (u, v, w)$

Greek

α	Angle of attack
$\vec{\phi}$	Orientation vector $\vec{\phi} = (\phi, \theta, \psi)$
$\dot{\vec{\phi}}$	Rotation rate vector $\dot{\vec{\phi}} = (p, q, r)$
ρ	Density

Subscripts

∞	Free stream values
exp	Measured values
sim	Simulated values

¹German Aerospace Center (DLR), Institute of Aerodynamics and Flow Technology, Spacecraft, Lilienthalplatz 7, 38108 Braunschweig, Germany, bodo.reimann@dlr.de

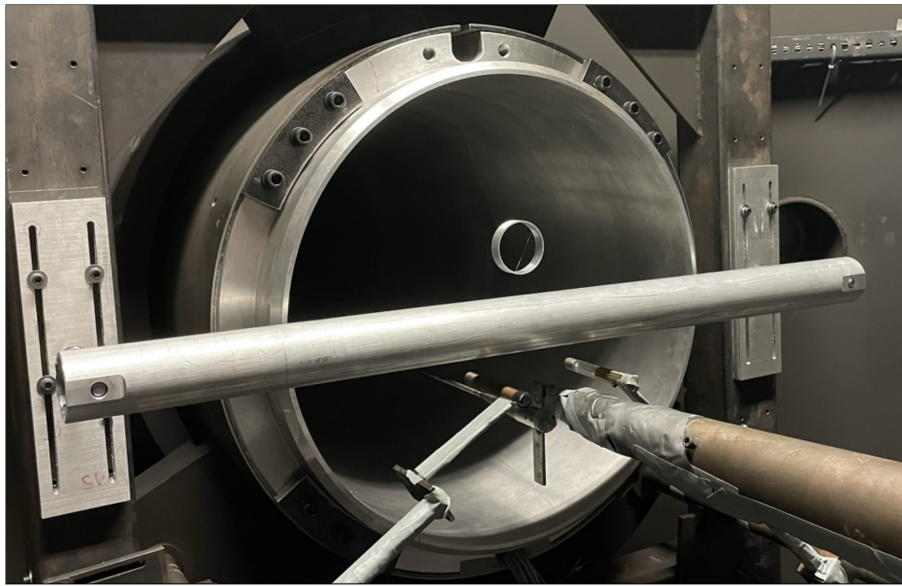


Fig 1. Experimental set-up in the VKI Longshot test section (taken from [1]).

1. Introduction

Discarded parts of past space missions remain in orbit for long periods of time before they enter the atmosphere uncontrolled, burn up, or partially hit the surface. These broken satellites, burnt out rocket stages, lost tool boxes or paint chips form a growing cloud of space debris around our planet. The size of the parts ranges for trackable ones from several meters to centimeters down to the fraction of a millimeter. Cascading collisions between these objects create new, smaller debris which in turn increase the likelihood of further collisions (Kessler effect). Even the tiniest parts possess huge kinetic energy due to their tremendous speed, and cause great damage in case of a collision with an active mission. In short, the garbage becomes a growing problem for space travel. The goal for the future must be to avoid further space debris. One way is to initiate the re-entry after the end of the operational period with a structural design that ensures the demise. The purpose of a design for demise is to break apart the structure and burn its components due to the high mechanical and thermal stresses during the flight. Software tools that can compute re-entry trajectories and possible ground footprints rely on simplified aerodynamic methods and correlations. These tools take not into account the interaction between different fragments, shock waves or complex geometries. For a better understanding of these effects the Aerothermodynamics & Design for Demise (ATD3) working group test case 2022 focuses on the aerodynamic behaviour and prediction of interacting free-flying bodies at hypersonic speed.

2. Test case description and experimental set-up

The selected test case consists of a free-flying annular ring crossing the oblique bow shock in front of a two-dimensional fixed cylinder. The test has been carried out in the VKI Longshot hypersonic gun tunnel using free-flight measurement technique at a free stream Mach number of 14. The scenario represents a generic interaction between an inter-stage adapter and a rocket stage during break-up and reentry. The experimental set-up and the results are discussed in detail by Kovács et al. [1] and [2]. Figure 1 shows the Longshot test section with the nozzle, the cylinder mounted in lateral direction, and the ring suspended by thin wires above the cylinder. When the flow builds up, the wires break and the ring flies freely in the test section and interacts with the oblique shock generated by the cylinder. The test time is in the range of a few milliseconds. During this time a number of schlieren pictures is taken. The trajectory, velocity and acceleration of the ring is reconstructed from the pictures using an optical tracking algorithm. Below the cylinder in Fig. 1 a set of probes is installed to measure static pressure and stagnation pressure and heat flux. Using a viscous correction of the measured static pressure, Rankine-Hugoniot's jump relation, and Fay-Riddell's formula for stagnation heat flux, the free stream

velocity and temperature are iterated from a first guess until they match the measured values [3]. The finale test case consists of a data set which contains free stream data, the position, and orientation and all velocities and accelerations of the ring, and the derived aerodynamic coefficients over time. The goal of the workshop was to provided numerical results of the free-flying ring and to compare them with the experimental results.

Both the cylinder and the ring have a outer radius of $R = 60 \text{ mm}$. The ring has a high of $h = 15 \text{ mm}$ and a thickness of $t = 2 \text{ mm}$. With the mass $m = 13.3 \text{ g}$ the symmetrical tensor of inertia with respect to the Center of gravity (GoG) is computed as

$$I_{yy} = I_{zz} = \frac{1}{12} m \left[3R^2 + 3(R-t)^2 + h^2 \right] \quad (1)$$

$$= 5.548675 \cdot 10^{-6} \text{ kg m}^2 \quad (2)$$

$$I_{xx} = \frac{1}{2} m \left[R^2 + (R-t)^2 \right] \quad (3)$$

$$= 11.1986 \cdot 10^{-6} \text{ kg m}^2 \quad (4)$$

$$I_{xy} = I_{xz} = I_{yz} = 0.0 \text{ kg m}^2 \quad (5)$$

A detailed analysis of the experiment showed that the wires holding the ring in its initial position did not break immediately with the start-up of the flow [2]. For the test case it was decided to start the numerical simulation at $t = 3.8 \text{ ms}$ after the arrival of the flow in the test section, at this time the ring is free. The motion state and free stream condition at this time is listed in Tab. 1. The complete time-history of free stream data taken from [1] is shown in Fig. 6. The test gas in the VKI facility is nitrogen, the Reynolds number is within the laminar flow regime.

Table 1. Initial condition for the numerical simulation.

t [ms]	u_∞ [mm]	ρ_∞ [g/m ³]	T_∞ [K]	x [mm]	z [mm]	u [m/s]	w [m/s]	θ [°]	q [°/s]
3.8	2530	5.02	82.6	-33.77	77.43	3.603	0.3525	-2.04	-483.75

3. Numerical scheme

The presented numerical results have been carried out with the DLR TAU code. The TAU flow solver [4, 5] is a cell centered finite volume method to solve the Euler or Navier-Stokes equations on unstructured grids. Based on a primary grid an edge-based dual-grid metric is generated in a preprocessing step. In the same step coarser levels of the dual-grid are agglomerated to accelerate numerical convergence using multi-grid technique. Domain splitting is also performed by the preprocessor in order to run parallel computations. In the CFD solver module inviscid terms are computed by employing an AUSMDV upwind scheme using linear reconstruction to get second-order spatial accuracy. Viscous terms are computed with a second-order central scheme. For time integration an explicit Runge-Kutta schemes, as well as an implicit approximate factorization lower-upper symmetric Gauss-Seidel scheme (LU-SGS) is implemented.

In order to perform simulations with moving grids TAU is written in an arbitrary Lagrangian-Eulerian formulation. The technique of overlapping grids [6] (Chimera technique) allows for the simulation of configurations with movable parts. The method handles the data exchange and interpolation in the overlapping regions. Grid regions that overlap solid parts have to be excluded from the flow computation. This is done by an automatic hole cutting procedure [7] which is based on the intersection of grid edges and surface cells to detect grid points inside solid bodies. Data exchange in surface boundary layers may cause interpolation errors due to large gradients and the insufficient resolution of the overlapping grid. To avoid this a procedure to adapt the location of the interpolation zone is implemented in order to minimize the width of the overlap, so that the interpolation boundaries are shifted away from the body surfaces. The current implementation of the Chimera technique covers multiple moving parts, and is also available for parallel simulations.

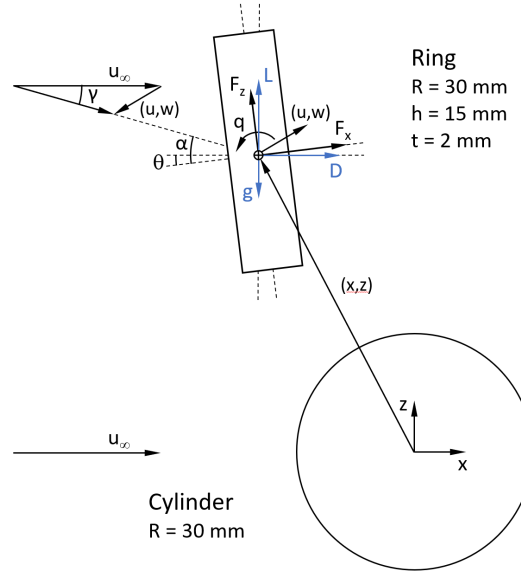


Fig 3. Dimensions of the configuration and coordinate systems.

motion, as well as the roll and yaw rotation are neglectable. For the simulations with prescribed motion or loads these values are zero anyway, as they are not included in the experimental data set. For these reasons only three degrees of motion (longitudinal, vertical, and pitch) will be consider. Lift and drag measured in the wind tunnel coordinate system then result from the body-fixed forces according to

$$D = F_z \sin \theta + F_x \cos \theta \quad (9)$$

$$L = F_z \cos \theta - F_x \sin \theta \quad (10)$$

and the corresponding coefficients are calculated according to

$$C_D = \frac{D}{q_\infty 2 R h} \quad (11)$$

$$C_L = \frac{L}{q_\infty 2 R h} \quad (12)$$

$$C_m = \frac{M_y}{q_\infty 2 R^2 h} \quad (13)$$

In the aerodynamic coordinate system the motion of the ring with respect to the free stream of the wind tunnel has to be considered for the computation of the dynamic pressure q_∞

$$q_\infty = \frac{1}{2} \rho_\infty \left[(u_\infty - u)^2 + w^2 \right] \quad (14)$$

and the angle of attack α as sum of the pitch angle θ and the flight path angle γ

$$\alpha = \theta - \gamma \quad \text{with} \quad \gamma = \arctan \left(\frac{w}{u_\infty - u} \right) \quad (15)$$

The pressure coefficient is defined as

$$C_p = \frac{p - p_\infty}{\frac{1}{2} \rho_\infty u_\infty^2} \quad (16)$$

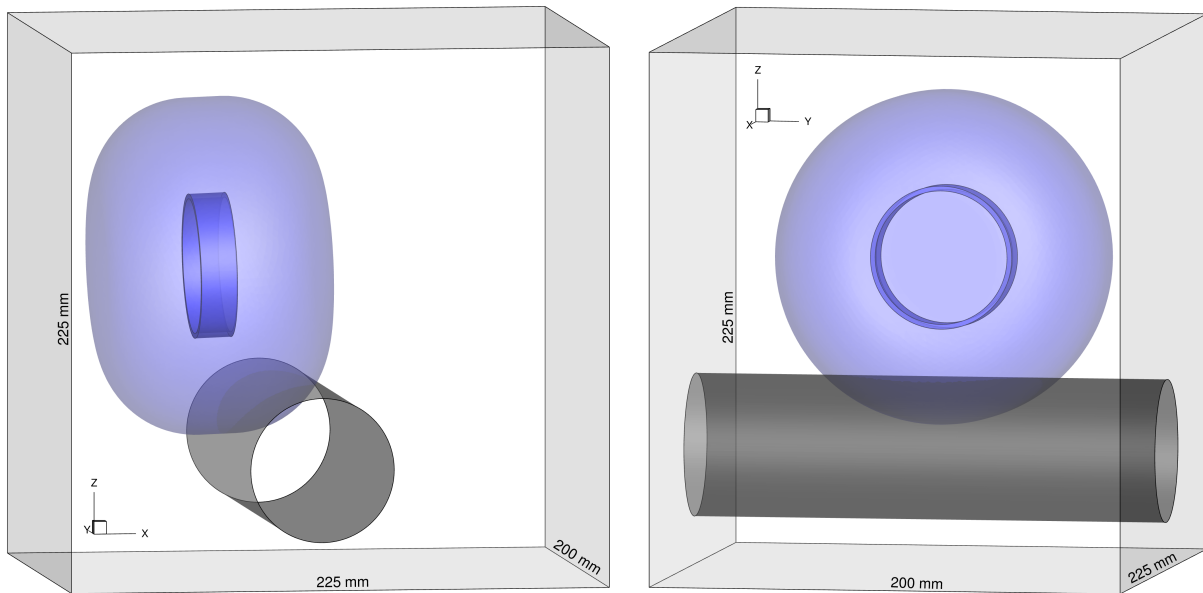


Fig 4. Computational domain. The domain consist of two overlapping sub-domains for the cylinder (grey) and the ring (blue).

The computational domain shown in Fig. 4 consist of a rectangular box of $225 \times 200 \times 225$ mm. The cylindrical sub-domain for the ring has a radius of 70 mm and height of 95 mm. The ring has the initial position and orientation given in Tab. 1. The domain is discretized using the commercial grid generation software CENTAUR . The initial mesh has around 790 thousand points and is dynamically adapted during the unsteady simulation to a minimum edge length of 0.1 mm and a maximum number of 20 million points. Figure 5 shows on the left hand side the center plain of the initial grid. On the right hand side the grid was locally refined to capture shock waves, furthermore regions of the grids that overlap solid bodies have been removed.

The unsteady coupled and forced motion simulations start from a converged flow field solution on a refined mesh using the initial conditions given in Tab. 1. In each time step the motion state and/or the aerodynamic field is computed depending on the used simulation type. At the end of the time step the grid is adapted to capture the new shock contours and the inflow condition is updated according to the measured free stream values shown in Fig. 6. In total 9.2 ms of physical time have been simulated from 3.8 ms to 13.0 ms. For the flight mechanic simulation only the motion state is computed. All simulations uses a time step of $\Delta t = 0.1$ ms. For the coupled simulations five coupling cycles have been completed. A time step convergence study with a time step of $\Delta t = 0.05$ ms shows no difference in the results. The test gas is to be assumed calorically perfect nitrogen, all body surfaces are modeled as non-slip isothermal boundaries with constant wall temperature of $T_{wall} = 300$ K. Sutherland's law is used to determine the temperature dependency of the viscosity.

5. Results

The results of all simulations and the experiment are compared in Fig. 8 and Fig. 9. While Fig. 8 shows the development of lift, drag, and pitching moment of the ring versus angle of attack (left) and versus time (right). Figure. 9 shows the time-history of horizontal and vertical position, the attitude, and the corresponding velocities of the ring. To illustrate the influence of the shock interaction on the motion and the aerodynamic forces on the ring (blue) additional coupled simulation results without the cylinder (red) are presented. In the case without shock interaction the ring moves with almost uniform acceleration.

During the entire test period the results of the fully coupled CFD/RBD simulation (solid blue lines) show

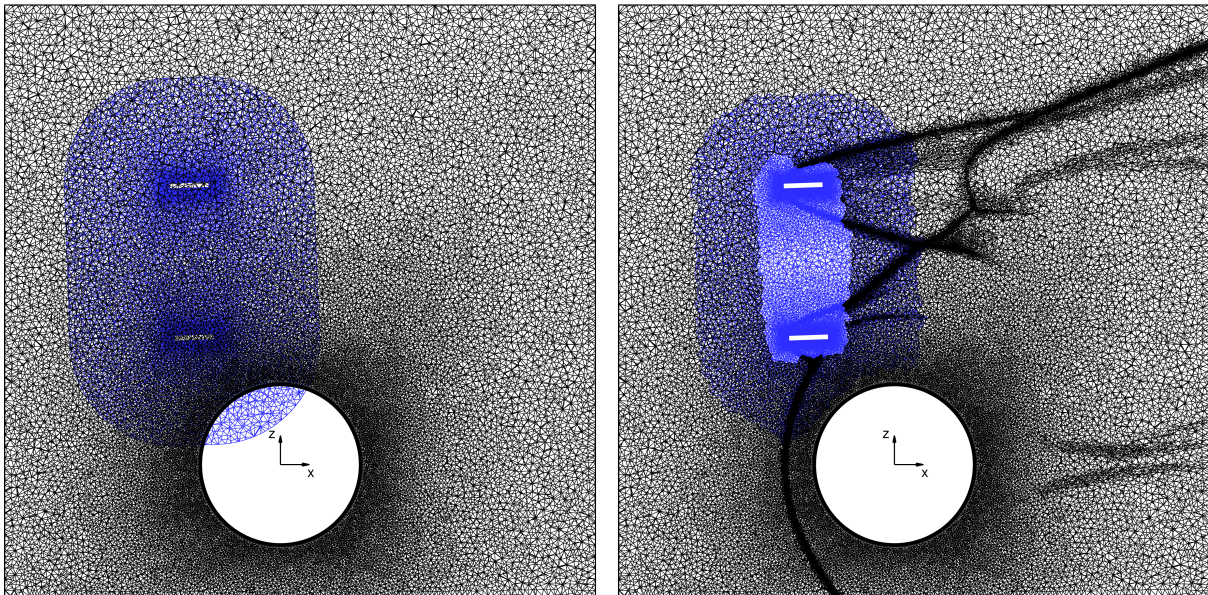


Fig 5. Center cut-plane of the primary computational mesh. Cylinder mesh with inertial coordinate system (black) and overlapping ring mesh (blue). The picture shows on the left the original mesh, and on the right a local refined mesh where the body overlapping parts have been removed.

up to 25% higher drag values compared to the measurements. Lift and pitching moment are also above the measured values until they reach their maximum values at $t = 8.3$ ms and $t = 8.1$ ms respectively. The comparison with the simulation without cylinder (solid red lines) shows that the bow shock of the cylinder already has an influence on the ring right at the start of the simulation at $t = 3.8$ ms. The change over time in the experimental values is also less pronounced compared to the computation. Not reproduced by the simulation is the bending of the curves of drag and pitching moment at $t = 11$ ms. The larger simulated forces lead to higher velocities and a greater distance covered by the ring in the same time, the difference in pitching moment leads to a smaller pitch angle both is shown in Fig. 9. A different positioning of the ring within the shock layer of the cylinder in turn influences the location and the type of the shock interaction and thus the surface pressure distribution and the acting forces and moments.

To separate these effects the results of a forced motion simulated (dashed blue line) prescribing the measured trajectory are compared in Fig. 8. Considering the distributions of the aerodynamic loads versus time both simulations show very similar results, the differences between the simulations are much smaller than the differences compared to the Longshot data. Considering the loads versus angle of attack the forced motion data show a shift towards higher (negative) angles and are closer to the measured points. The angle of attack is a time dependent variable and the shift is due to the fact that the pitch angle from the forced simulation is always smaller than the pitch angle computed by the coupled simulation. Despite identical movement of the ring in the forced motion simulation and the experiment the simulated forces are still much higher.

The results of the steady-state computations (circles) are consistent with the unsteady results, slight differences are due to the fact that the ring is not moving. The differences between the various simulations on the trajectory of the ring is also shown qualitatively in Fig. 7. On the left fully coupled (grey) and forced motion (blue) results are shown. The right side highlight the effect of the shock interaction between coupled results (grey) and results without cylinder (red).

The flight mechanic simulation using the measured aerodynamic loads was intended to check the consistency of the experimental data set and the 6-DoF solver. Position, orientation and the corresponding velocities of the ring versus time are plotted in Fig. 9. The calculated curves (dashed lines) show good

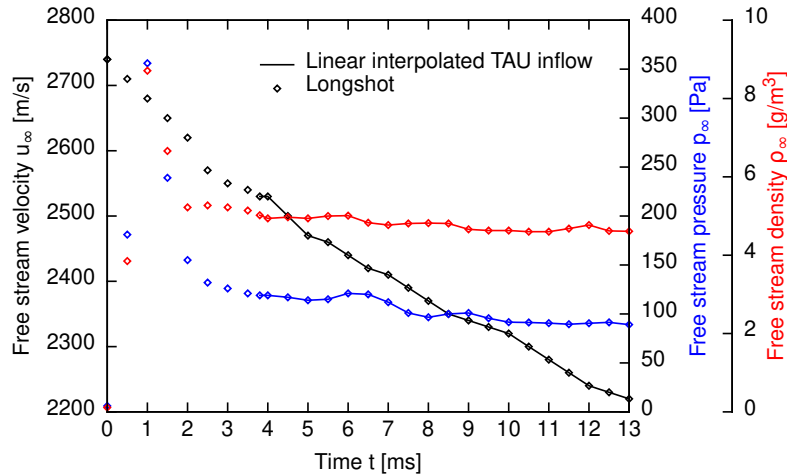


Fig 6. Time-history of the measured free stream values in the VKI Longshot gun tunnel (data taken from [1]). A linear interpolation is used to determine the TAU inflow boundary condition.

agreement and are largely within the error range of the measured data. The sensitivity of the motion state have been investigated including the given upper and lower error of the forces and moments (diamonds in Fig. 8) in the 6-DoF simulation. The results are within the blue areas. The error add up over time and are therefore significantly larger than the errors of the direct measured values. The computed pitch angle and pitch rate are almost everywhere within this error range, that is not the case for the horizontal and vertical translational motion.

Figure 10 shows a series of simulation results of the coupled CFD/RBD simulation. Shown is the distribution of the surface pressure coefficient C_p and a schlieren image reconstructed from the density gradient in the center plane of the computational domain. In hypersonic flow the majority of the force is pressure-induced, so the C_p distribution is an indicator for the forces. As far as the ring enters the shock layer of the cylinder the interaction between the cylinder shock and the ring shock lead to a growing region of high pressure on the lower outer side of the ring which is responsible of the lift increase up to $t = 8.3$ ms. At this time the secondary interaction point reaches the stagnation region of the ring. The observed Edney type interaction increase the pressure on the thin front side of the ring up to a maximum value of $C_p \approx 6$. This pressure rise initiates the increase of the drag and the pitch down motion. When the interaction moves upwards, the pressure on the outer side and thus the lift decreases again.

6. Conclusion

Fully coupled CFD/RBD and forced motion simulations have been carried out to reproduce the VKI experiment of a free-flying ring crossing the curved shock wave in front of a cylinder. Both simulations show to high values for lift and drag compared to the measurements. The simulations also show a faster change of the values and can not reproduce the drag decrease and the pitching moment increase towards the end of the test time. One source for the less pronounced gradients could be the filtering of the experimental data. A Savitzky-Golay filter have been applied to the data. Not clear is if the filtering is also responsible for the bending of the curves at the end. Fact is that ring leaves the core flow of the VKI Lonshot nozzle and interacts with the shear layer [2], which should account for the majority of the effect. The higher force values may be caused by different free stream values in the wind tunnel test and in the simulations or an inadequate gas model. A calorically perfect gas model is applied, neither thermo-chemical excitation of the nitrogen molecules in the nozzle reservoir nor freezing during the expansion process are taken into account. Some aspects of the calibration and the modeling of the

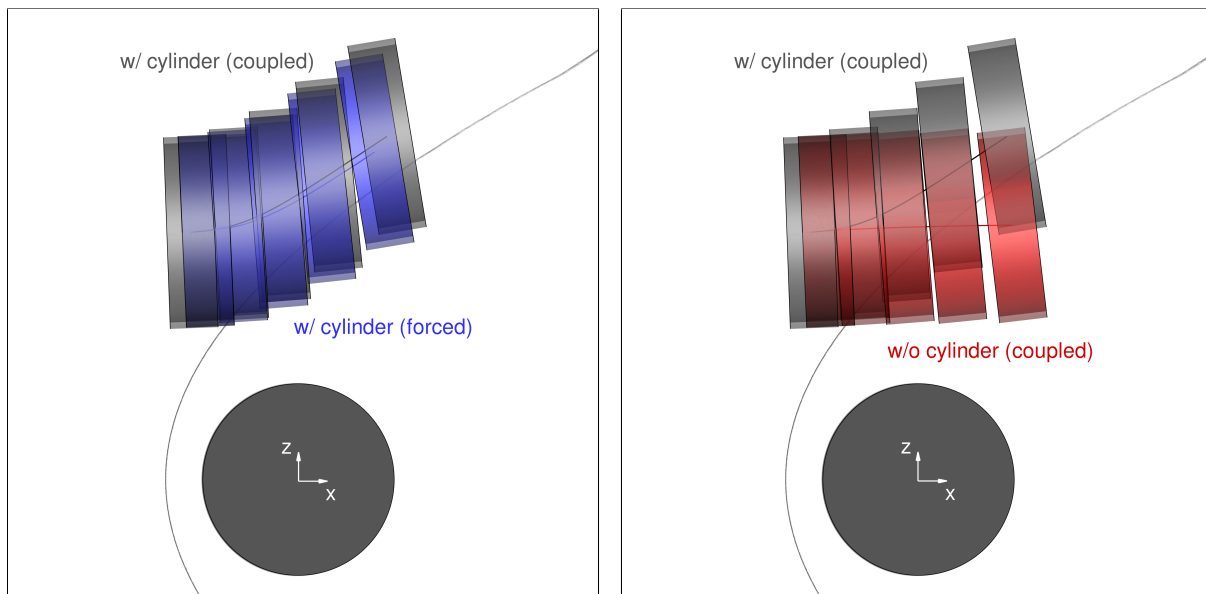


Fig 7. Difference in position and attitude of the ring between coupled (grey) and forced motion (blue) simulation results (left). The force motion results are identical to the measured VKI Longshot data. Influence of the shock interaction on the position and attitude of the ring (right). Shown is the initial position at 3.8 ms and results at 5.0 ms, 7.0 ms, 9.0 ms, 11.0 ms, and 13.0 ms.

Longshot nozzle expansion including the effects of non-perfect and dense gas corrections are discussed in [10] and [11]. The fact that the experimental data set is based only on one single experiment is not optimal, data from several experiments would allow to estimate the shot to shot variation regarding the initial and boundary (free stream) conditions.

References

- [1] Kovács, D. G., Grossir, G., and Chazot, O.: Hypersonic aerodynamics of a free-flying ring interfering with a two-dimensional curved shock wave - An experimental test case. 2nd International Conference on Flight Vehicles, Aerothermodynamics, and Re-entry Missions & Engineering (FAR 2022), 19–23 June, Heilbronn, Germany (2022)
- [2] Kovács, D. G., Grossir, G., and Chazot, O.: Space debris interaction across a two-dimensional oblique shock wave. *Experiments in Fluids* **64**, 146 (2023) <https://doi.org/10.1007/s00348-023-03686-9>
- [3] Grossir, G. and Dias, B.: Flow characterization of the VKI Longshot wind tunnel. *Flow Characterization and Modeling of Hypersonic Wind Tunnels*, STO-AVT 325, pp. 1–32, von Karman Institute for Fluid Dynamics, Rhode-St-Genése, Belgium (2018)
- [4] Schwamborn, D., Gerhold, T., and Heinrich, R.: The DLR TAU-Code: Recent Applications in Research and Industry, ECCOMAS CFD 2006, 5–8 September, Eggmond aan Zee, The Netherlands (2006)
- [5] Mack, A. and Hannemann V.: Validation of the Unstructured DLR-TAU-Code for Hypersonic Flows. 32nd AIAA Fluid Dynamics Conference and Exhibit, 24–26 June, AIAA Paper 2002-3111, St. Louis, Missouri, USA (2002) <https://doi.org/10.2514/6.2002-3111>
- [6] Madrane, A., Raichle, A., and Stürmer, A., Parallel Implementation of a Dynamic Overset Unstructured Grid Approach, ECCOMAS 2004, 24–28 July, Jyväskylä, Finland (2004)

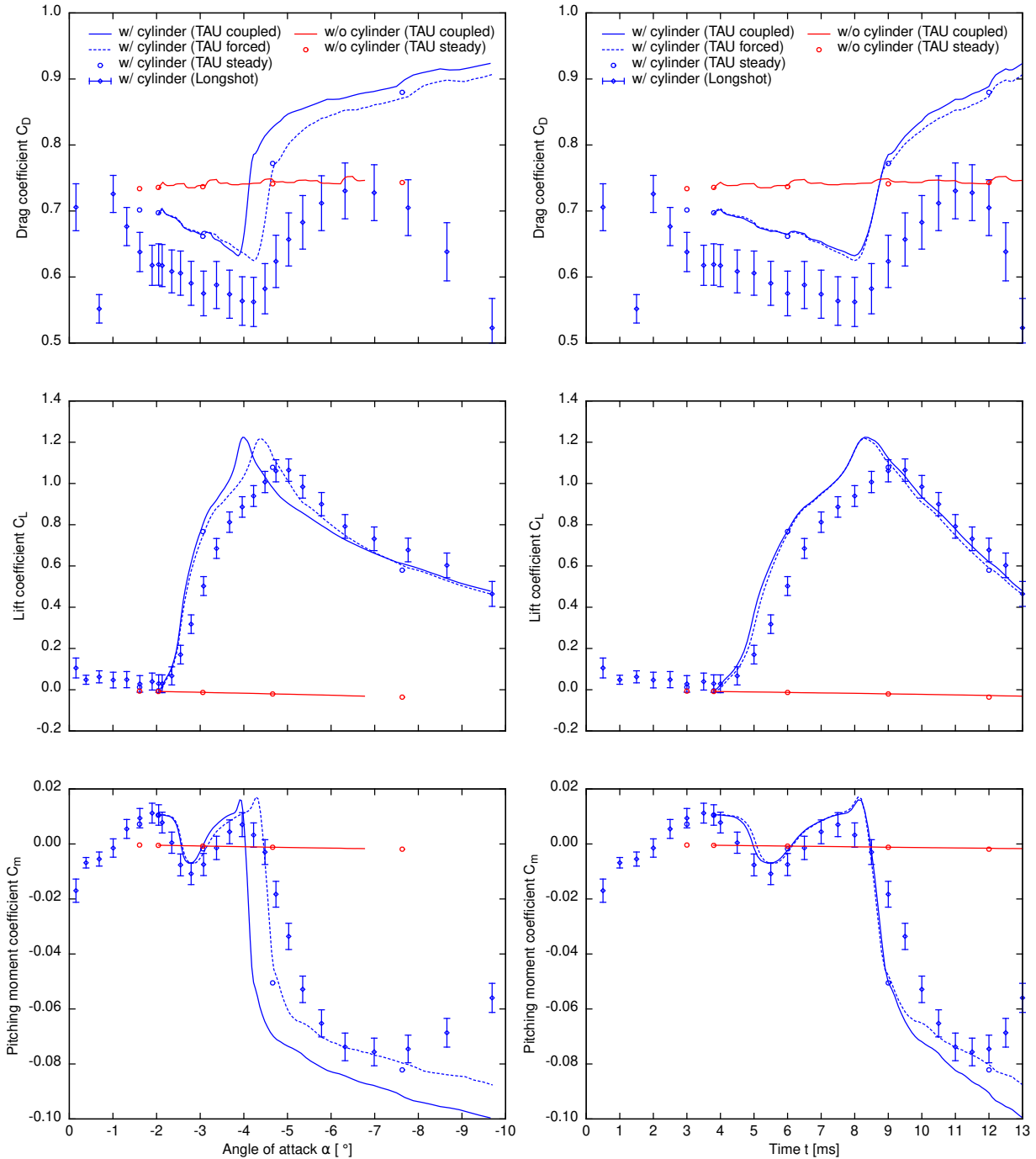


Fig 8. Comparison of simulated (lines) and measured (diamonds) aerodynamic coefficients of the annular ring interacting with the bow shock in front of the cylinder (blue) and without shock interaction (red). Shown are results received with CFD/RBD coupling (solid lines) and forced motion results (dashed lines). The steady-state results (circles) have been simulated at a fixed time using the conditions at 3.0 ms, 3.8 ms, 6.0 ms, 9.0 ms, and 12.0 ms (left to right) after flow onset.

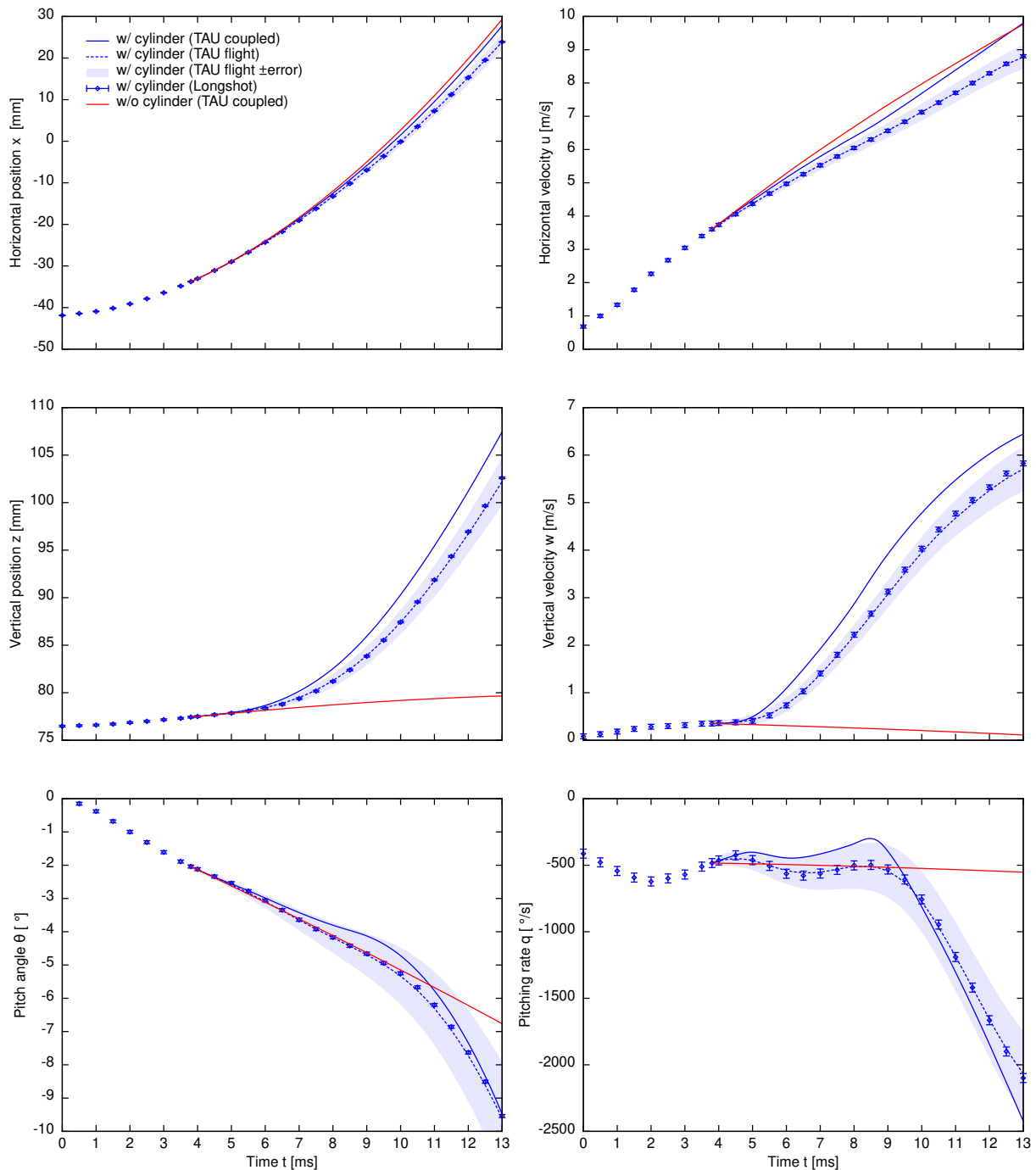


Fig 9. Comparison of the simulated (lines) and measured (diamonds) motion state of the annular ring interacting with the bow shock in front of the cylinder (blue) and without shock interaction (red). Shown are results achieved with CFD/RBD coupling (solid lines) and result achieved with the flight mechanic solver and prescribed loads (dashed lines). In addition flight mechanic results along the upper and lower error limits of the prescribed loads by are shown (blue area).

- [7] Spiering, F., Development of a Fully Automatic Chimera Hole Cutting Procedure in the DLR TAU Code, *Notes on Numerical Fluid Mechanics an Multidisciplinary Design* **132**, pp. 585–595, Springer (2016)
- [8] Heinrich, R., Reimer, L., and Michler, A.: Multidisciplinary simulation of maneuvering aircraft interacting with atmospheric effects using the DLR TAU code, RTO AVT-189 Specialists' Meeting on Assessment of Stability and Control Prediction Methods for Air and Sea Vehicles, 12–14 October, Portsmouth West, UK (2011)
- [9] Reimer, L., Heinrich, R., and Meurer, R., Validation of a Time-Domain TAU-Flight Dynamics Coupling Based on Store Relation Scenarios, *Notes on Numerical Fluid Mechanics an Multidisciplinary Design* **124**, pp. 455–463, Springer (2014)
- [10] Kovács, D. G., Ilich, Z., Grossir, G., and Chazot, O.: Experimental Characterization of the VKI Longshot Mach 14 Contoured Nozzle. AIAA SciTech Forum 2022, 3–7 January, AIAA Paper 2022-1401, San Diego, California, USA (2022) <https://doi.org/10.2514/6.2022-1401>
- [11] Geratz, M., Capriati, M., Grossir, G., and Magin, T. E.: Influence of Physical Models on the Numerical Modeling of Hypersonic Nozzle Flow Expansion. 9th European Conference for Aeronautics and Space Sciences, EUCASS Paper 2022-6142, 27 June – 1 July, Lille, France (2022) <https://doi.org/10.13009/EUCASS2022-6142>
- [12] Reimann, B., Simulation of Support Module Separation in a Hypersonic Flight Experiment, 1st International Conference on High-Speed Vehicle Science Technology HiSST 2018, 26–29 November, Moscow, Russia (2018)

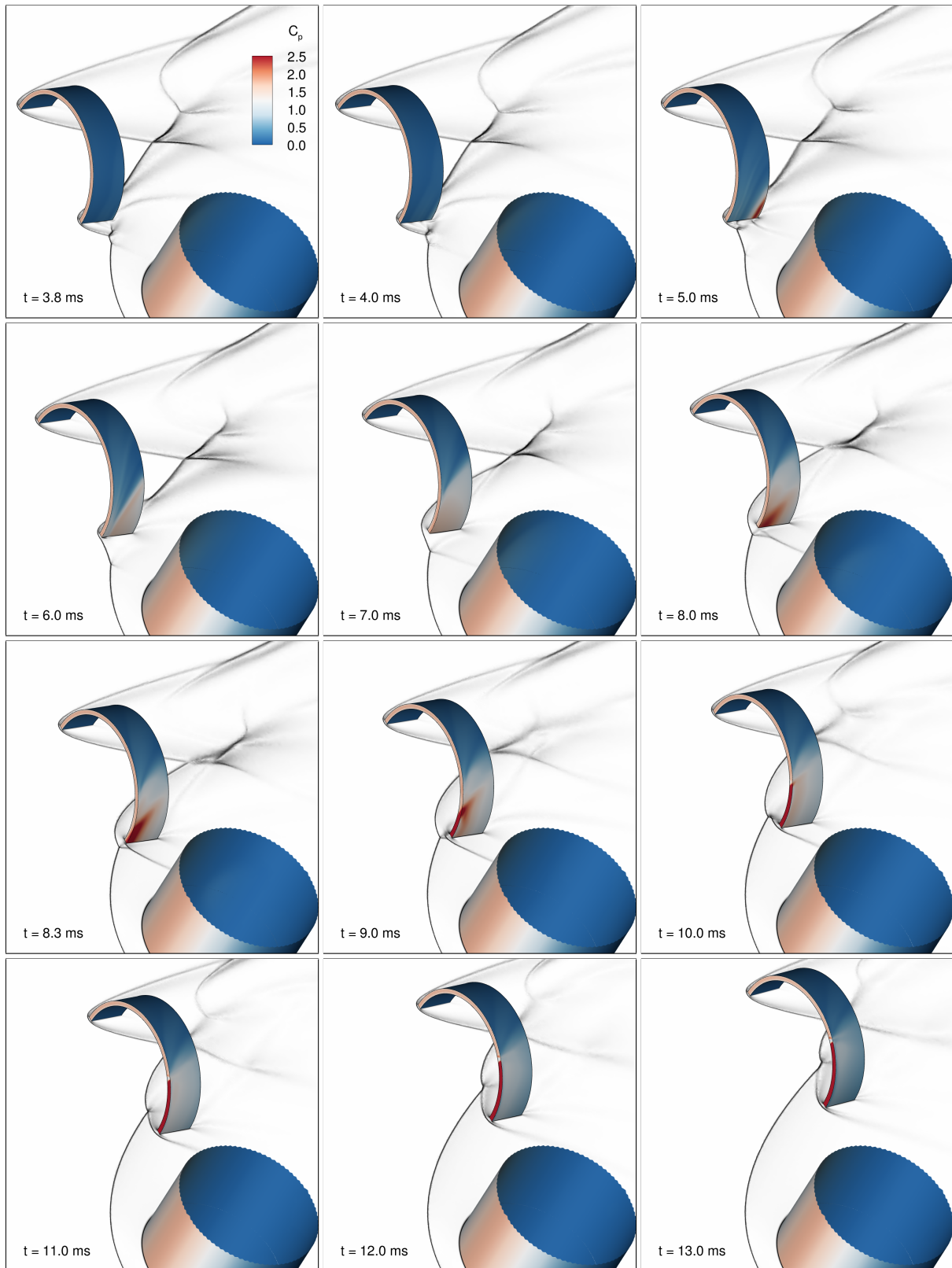


Fig 10. Computed surface pressure coefficient C_p and center plane schlieren pictures showing the motion of the ring and the interaction between the shock waves. The results have been achieved with the coupled CFD/RBD simulation. The simulated time is from $t = 3.8$ ms (initial solution) to 13 ms. Maximum lift is reached at $t = 8.3$ ms. The maximum reached pressure coefficient is about $C_p \approx 6$.