



Study of Detonation Waves by Means of Mathematical Modeling

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Abstract

Keywords: three-dimensional nonstationary flow, rotating detonation, numerical study

1. Introduction

According to experimental data and the results of theoretical studies, the existence of self-sustained waves of gas detonation is associated with nonstationary processes and the formation of periodic flow structures [1-3]. Numerical studies of the initiation of detonation in the one-dimensional approximation revealed a nonstationary wave structure of detonation. According to calculations, such a wave is always nonstationary, and the wave velocity and parameters on its leading edge vary periodically under the influence of shock waves formed in the induction zone ahead of the accelerating front of flame [4-7]. It turned out that an autooscillatory process develops only when the value of the initiation energy exceeds a certain critical value. Otherwise, the detonation wave decays, decaying into a shock wave and a wave of slow combustion. The values of the critical energy at initiation of detonation were determined various external sources of energy [8-11], as well as the possibility of initiation of detonation as a result of the collapse of a spherical or cylindrical region with reduced pressure without additional energy supply from outside [12-14]. According to the results of calculations of the development of a local perturbation of a plane wave, in the two-dimensional approximation, instead of longitudinal one-dimensional waves, transverse waves are formed and the cellular structure observed in the experiments [15]. The two-dimensional spin model used by many researchers was formulated, and the structure of a two-headed spin detonation wave was calculated [7]. Wave processes were studied during detonation both in a hydrogen-air mixture at rest and in a supersonic flow [16-19]. Special attention was paid in the last decade to problems of initiation and stabilization of detonation in limited volumes of combustion chambers of power plants that realize high-speed combustion of fuel. The use of high-performance computer technology made it possible to investigate multidimensional flows during the initiation of detonation due to the energy of the motion of the combustible mixture and in its interaction with moving boundaries [20-24]. In this case, previously unknown modes of propagation of waves of chemical reactions, including galloping layered detonation, were detected. A detailed numerical study of the formation and stability of three-dimensional spin detonation is carried out [25]. The most promising from the point of view of practice is a rotating detonation. In this connection, it draws special attention to both experimentalists and theoreticians [26]. Currently, the development and creation of power plants are associated with the use of methods of mathematical modeling using a multiprocessor computer techniques. This article presents the results of numerical studies of the combustion of propane-air mixture in a rotating detonation wave in a device of a special design. For calculations, the supercomputer of the Lomonosov Moscow State University was used [27], where earlier three-dimensional non-stationary reacting flows were calculated on grids with billions of computed cells. Similar calculations of rotating detonation were performed for the first time in Russia. Similar problems are dealt with in the Institute of Hydrodynamics. M.A. Lavrent'ev, Siberian Branch of the Russian Academy of Sciences, where a series of experimental and theoretical studies devoted to combustion chambers with rotating detonation was carried out.

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2. Detonation in the annular gap

The problem of a three-dimensional nonstationary flow with a rotating detonation wave arising in the annular gap of an axisymmetric device between two parallel planes perpendicular to its axis of symmetry is investigated. It is assumed that a homogeneous combustible propane-air mixture, resting in a reservoir with predetermined braking parameters, enters the annular gap through its outer cylindrical surface towards the axis of symmetry and its parameters are determined by the pressure in the reservoir and the static pressure in the gap. The detonation products flow out of the gap into space, bounded on one side by an impenetrable wall—the continuation of the side of the gap. Through the hole in the other side of the gap and the conical exit section with the angle of half-solution 45, the gas flows out of the device into the outer space. The model of detonation initiation by the energy supply is formulated, in which the direction of rotation of the detonation wave is determined by the location of the energy release zone of the initiator relative to the solid wall located in the plane passing through the axis of symmetry. After a certain time, this solid wall disappears (burns). Nonstationary shock-wave structures arising in the process of formation of a stationary rotating detonation are obtained and analyzed. To describe gasdynamic three-dimensional unsteady flows, the Euler equations system for an ideal multicomponent reacting mixture in a fixed Cartesian coordinate system is used. The detonation of a stoichiometric propane-air mixture in the framework of a one-stage kinetics with one irreversible reaction is considered [28]. The study is carried out by the modified method of S.K. Godunov [29] of the first order of accuracy with respect to space and time. The method is implemented in the original software package designed to solve a wide range of one-dimensional, two-dimensional and three-dimensional problems of non-stationary dynamics of gaseous combustible mixtures. The software complex has a graphical interface with visualization functions. The computational algorithm is parallelized on the basis of MPI and allows the calculation of tasks with the number of calculated cells of several billion. In this paper, we present the results obtained on a supercomputer of the Lomonosov Moscow State University with calculated grids containing 0.1 to 10 billion cells.

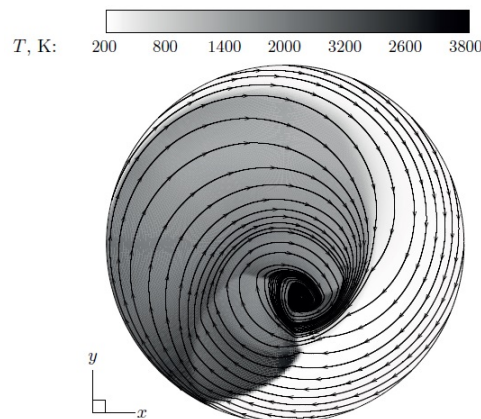
A series of calculations was carried out, which made it possible to obtain optimal values for the parameters of the initiators of rotating detonation. It is established that a rotating detonation wave is formed in the chamber, the direction of rotation of which is determined by the location of the energy release zone of the initiator relative to the solid wall, in the plane passing through the axis of symmetry. After a certain time, this solid wall disappears (burns). Nonstationary shock-wave structures arising in the process of formation of a stationary rotating detonation are obtained and analyzed.

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Below, the figure shows the temperature field for steady-state rotation of the detonation. On it are superimposed streamlines constructed in a coordinate system rotating with the wave. In this figure, a vortex zone is visible and the current lines on shock waves are refracted. All streamlines emerge from the boundary circle at the same angle, determined by the ratio of the leak-in rate and the linear velocity during the rotation of the detonation. In the restricted zone, there is no inflow behind the detonation wave and the streamlines are parallel to the boundary circle. In the figure, the contact surface between the shock waves b and e is visible. It separates a dark zone with an elevated temperature and a dense arrangement of streamlines and a light zone of a heated mixture in which

the streamlines are more sparse. It is clearly seen that the contact surface in question coincides with one of the spiral streamlines ending at the center of the vortex zone.



Temperature field with current lines for steady-state rotation of detonation. Current Lines are constructed in a coordinate system rotating with the wave.

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